## Cambridge IGCSE ${ }^{\text {TM }}$

CAMBRIDGE INTERNATIONAL MATHEMATICS 0607/41
Paper 4 (Extended)
May/June 2022
MARK SCHEME
Maximum Mark: 120

## Published

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge International will not enter into discussions about these mark schemes.
Cambridge International is publishing the mark schemes for the May/June 2022 series for most
Cambridge IGCSE, Cambridge International A and AS Level and Cambridge Pre-U components, and some Cambridge O Level components.

## Generic Marking Principles

These general marking principles must be applied by all examiners when marking candidate answers. They should be applied alongside the specific content of the mark scheme or generic level descriptors for a question. Each question paper and mark scheme will also comply with these marking principles.

## GENERIC MARKING PRINCIPLE 1:

Marks must be awarded in line with:

- the specific content of the mark scheme or the generic level descriptors for the question
- the specific skills defined in the mark scheme or in the generic level descriptors for the question
- the standard of response required by a candidate as exemplified by the standardisation scripts.


## GENERIC MARKING PRINCIPLE 2:

Marks awarded are always whole marks (not half marks, or other fractions).

## GENERIC MARKING PRINCIPLE 3:

Marks must be awarded positively:

- marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit is given for valid answers which go beyond the scope of the syllabus and mark scheme, referring to your Team Leader as appropriate
- marks are awarded when candidates clearly demonstrate what they know and can do
- marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

GENERIC MARKING PRINCIPLE 4:
Rules must be applied consistently, e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

## GENERIC MARKING PRINCIPLE 5:

Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

GENERIC MARKING PRINCIPLE 6:
Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

Maths-Specific Marking Principles
Unless a particular method has been specified in the question, full marks may be awarded for any correct method. However, if a calculation is required then no marks will be awarded for a scale drawing.

2 Unless specified in the question, answers may be given as fractions, decimals or in standard form. Ignore superfluous zeros, provided that the degree of accuracy is not affected.

3 Allow alternative conventions for notation if used consistently throughout the paper, e.g. commas being used as decimal points.

4 Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored (isw).

5 Where a candidate has misread a number in the question and used that value consistently throughout, provided that number does not alter the difficulty or the method required, award all marks earned and deduct just 1 mark for the misread.

Recovery within working is allowed, e.g. a notation error in the working where the following line of working makes the candidate's intent clear.

## MARK SCHEME NOTES

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

## Types of mark

M Method marks, awarded for a valid method applied to the problem.
A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. For accuracy marks to be given, the associated Method mark must be earned or implied.

B Mark for a correct result or statement independent of Method marks.
When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. The notation 'dep' is used to indicate that a particular M or B mark is dependent on an earlier mark in the scheme.

## Abbreviations

| awrt | answers which round to |
| :--- | :--- |
| cao | correct answer only |
| dep | dependent |
| FT | follow through after error |
| isw | ignore subsequent working |
| nfww | not from wrong working |
| oe | or equivalent |
| rot | rounded or truncated |
| SC | Special Case |
| soi | seen or implied |


| Question | Answer | Marks | Partial Marks |
| :---: | :--- | ---: | :--- |
| 1(a) | $\begin{array}{l}\text { correct triangle } \\ (-4,1)(-3,1)(-3,1.5)\end{array}$ | $\mathbf{2}$ | B1 for translation $\binom{k}{2}$ or $\binom{-2}{k}$ or |
| $k$ |  |  |  |$)$


| Question | Answer |  |  | Marks | Partial Marks |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 3(d) | $-2.31 \leqslant x<0$ and $0<x \leqslant 0.388$ |  |  | 4 | $\begin{aligned} & \text { B3 for }-2.3 \leqslant x \leqslant 0.388 \\ & \text { or }-2.31 \leqslant x \leqslant 0.39 \\ & \text { or } \mathbf{B 2} \text { for }-2.3 \leqslant x \leqslant 0.39 \\ & \text { or }-2.31 \leqslant x \text { or } x \leqslant 0.388 \\ & \text { or } \mathbf{B 1} \text { for }-2.31 \text { or } 0.388 \text { seen } \\ & \text { or for correct sketch } \end{aligned}$ |
| 4(a) | 180 |  |  | 2 | $\text { M1 for } \frac{216}{5+1}[\times 5]$ |
| 4(b) | 741 |  |  | 2 | $\mathbf{M 1} \text { for } \frac{171}{3}$ |
| 4(c) | 1505 |  |  | 3 | M2 for $1400+3\left(1400 \times \frac{2.5}{100}\right)$ oe or M1 for $3\left(1400 \times \frac{2.5}{100}\right)$ oe |
| 4(d)(i) | 3247.30 or 3250 |  |  | 2 | M1 for $3000 \times\left(1+\frac{2}{100}\right)^{4}$ oe |
| 4(d)(ii) | 15 |  |  | 4 | B3 for 14.5 or 14.52 to 14.53 seen or M3 for $n \log (1.02)=\log \left(\frac{4000}{3000}\right)$ oe or for correct trials reaching 14 and 15 or good sketch indicating value between 14 and 15 <br> or M2 for $1.02^{n}=\frac{4000}{3000}$ or at least three correct trials for $n>4$ or suitable graph <br> or M1 for $3000 \times 1.02^{n}=4000$ soi by at least 2 correct trials for $n>4$ |
| 5(a) | $\begin{aligned} & 14 \\ & \hline 6 \end{aligned}$ | $\begin{array}{\|l\|} \hline 18 \\ \hline 12 \\ \hline \end{array}$ | $\begin{array}{\|l} 4 n+2 \mathrm{oe} \\ \hline n^{2}-n \mathrm{oe} \end{array}$ | 6 | B2 for all four numbers correct or B1 for at least two correct B2 for $4 n+2$ oe or M1 for $4 n+k$ B2 for $n^{2}-n$ oe or M1 for any quadratic or for second differences of 2 seen |
| 5(b) | $n^{2}+3 n+2$ or $(n+1)(n+2)$ |  |  | 1 | FT their grey + white if both in terms of $n$ |


| Question | Answer | Marks | Partial Marks |
| :---: | :---: | :---: | :---: |
| 5(c) | 94 | 4 | M1 for their $k^{2}+3 k+2=600$ oe M1 for correct method for solving their quadratic <br> M1 for substituting their positive integer (from a quadratic) $k$ into their $4 n+2$ |
| 5(d) | $\frac{343}{1728} \text { oe }$ | 2 | M1 for $\left(1-\frac{5}{12}\right)^{3}$ oe |
| 5(e) | $\frac{56}{153} \text { oe }$ | 3 | FT their 18 from (a) for M marks only M2 for $\frac{4}{18} \times \frac{14}{17}+\frac{14}{18} \times \frac{4}{17}$ oe <br> M1 for one product |
| 6(a) | 26.5 or 26.47 to 26.48 | 4 | B1 for $\angle A O C=150$ or $\angle B O C=75$ soi M1 for $\frac{\text { their } 150 \times \pi \times 5^{2}}{360}$ or $\frac{\text { their } 75 \times \pi \times 5^{2}}{360} \times 2$ <br> M1 for $\frac{1}{2} \times 5 \times 5 \times \sin [$ their 150$]$ or $\frac{1}{2} \times 5 \times 5 \times \sin [$ their $75 \times 2]$ |
| 6(b) | $5.5[0]$ or 5.49 to 5.51... | 5 | M2 for $\frac{(360-40)}{360} \times 2 \times \pi \times 12=2 \pi r$ oe or $\frac{(360-40)}{360} \times \pi \times 12^{2}=\pi r 12$ oe or M1 for $\frac{(360-40)}{360} \times 2 \times \pi \times 12$ or $\frac{(360-40)}{360} \times \pi \times 12^{2}$ <br> If minor sector $\mathbf{S C} 1$ for radius $=\frac{4}{3}$ oe <br> AND <br> M2 for $12^{2}$ - their (radius) ${ }^{2}$ oe dependent on at least M1 or SC1 or M1 for $h^{2}+$ their $(\text { radius })^{2}=12^{2}$ oe dependent on at least M1 or SC1 |
| 7(a) | 2300 | 2 | M1 for $2 \times 23 \times 50$ oe |


| Question | Answer | Marks | Partial Marks |
| :---: | :---: | :---: | :---: |
| 7(b)(i) | 4.6 | 3 | M2 for $1.15 \times \sqrt[3]{\frac{18400}{287.5}}$ oe or M1 for $\frac{h^{3}}{1.15^{3}}=\frac{18400}{287.5}$ or $\sqrt[3]{\frac{18400}{287.5}}$ or $\sqrt[3]{\frac{287.5}{18400}}$ seen |
| 7(b)(ii) | 2 : their (b)(i) or their (a) : 18400 soi | M1 | FT their figures |
|  | showing comparison of length ratio or volume ratio | M1 |  |
|  | not similar | A1 | Dep on M1M1 |
| 8(a) | 27.6 or 27.58 to 27.59 | 3 | M2 for $((-11)-8)^{2}+(7-(-13))^{2}$ oe or M1 for $((-11)-8)$ or $(7-(-13))$ oe |
| 8(b) | $y=-\frac{1}{4} x+8 \frac{1}{4}$ oe | 6 | B5 for answer $-\frac{1}{4} x+8 \frac{1}{4}$ <br> OR <br> B2 for (5, 7) <br> or B1 for $(5, k)$ or $(k, 7)$ <br> M1 for $\frac{11--5}{6-2}$ oe ( $=\mathrm{m}_{1}$ ) <br> M1 for grad $=-\frac{1}{\text { their } m_{1}}$ <br> M1 for substituting their $(5,7)$ into $y=($ their $m) x+c$ |
| 9(a)(i) | 13 | 1 |  |
| 9(a)(ii) | $-8 x-10$ oe final answer | 2 | M1 for $2-4(2 x+3)$ or better seen |
| 9(a)(iii) | $\frac{2-x}{4}$ oe final answer | 2 | M1 for correct first step $\begin{aligned} & y+4 x=2 \text { or } \frac{y}{4}=\frac{1}{2}-x \text { or } x=2-4 y \\ & y-2=-4 x \end{aligned}$ |
| 9(a)(iv) | 3.52 or 3.523 to 3.524 or $\log _{3} 48$ or $\frac{\log 48}{\log 3}$ | 2 | M1 for $\log 48=\log 3^{x}$ or better or suitable sketch |


| Question | Answer | Marks | Partial Marks |
| :---: | :---: | :---: | :---: |
| 9(b)(i) |  | 1 |  |
| 9(b)(ii) | $2 \mathrm{~m}(x)$ | 1 |  |
| 10(a) | $16 x y^{2}$ Final answer | 2 | M1 for $\frac{4 x^{2} y}{3} \times \frac{12 y}{x}$ or better |
| 10(b) | $\frac{-x^{2}+6 x-7}{2(x-3)}$ Final answer | 3 | B1 for $2[\times 1]-(x-3)(x-3)$ <br> B1 for $2(x-3)$ as denominator |
| 10(c) | $\begin{aligned} & 2^{2} \times a+2 \times b-5=-3 \mathrm{oe} \\ & 3^{2} \times a+3 \times b-5=4 \mathrm{oe} \end{aligned}$ | M2 | M1 for either |
|  | correctly equating one set of coefficients or making $a$ or $b$ subject of one equation | M1 | FT |
|  | correct method for eliminating one variable or correctly substituting in other equation | M1 | FT |
|  | $\begin{aligned} & {[a=] 2} \\ & {[\mathrm{~b}=]-3} \end{aligned}$ | B2 | B1 for each |
| 11(a) | 349 or 350 or 349.4 to $349.5 \ldots$ | 4 | M3 for <br> $\left[0.9 \times 2.1+2 \times \frac{1}{2}(2.1 \times 2.1 \tan 20)\right] \times$ <br> 100 oe <br> or $\frac{1}{2}(0.9+(2 \times 2.1 \tan 20+0.9)) \times 2.1 \times$ <br> 100 oe <br> or M2 for area of cross section <br> $0.9 \times 2.1+2\left[\frac{1}{2}(2.1 \times 2.1 \tan 20)\right]$ oe <br> or $\frac{1}{2}(0.9+(2 \times 2.1 \tan 20+0.9)) \times 2.1$ <br> oe <br> or $\mathbf{M 1}$ for $\tan 20=\frac{x}{2.1}$ <br> If 0 scored $\mathbf{S C 1}$ for triangle marked/drawn with 20 or 70 |


| Question | Answer | Marks | Partial Marks |
| :---: | :---: | :---: | :---: |
| 11(b) | 19 h 50 (or 51) min | 4 | B3 for 19.8 or 19.84... <br> or M2 for $\frac{300 \times 1000}{4.2 \times 60 \times 60}$ oe <br> or M1 for $300 \times 1000$ or $4.2 \times 60 \times 60$ <br> or for their volume divided by their rate |
| 12(a) | 160 or $159.5 \ldots$ | 2 | M1 for $\frac{1}{2} \times 16 \times 22 \times \sin 115$ oe |
| 12(b) | 84 [.0] or 84.02 to 84.03 | 6 | B3 for 32.2 or 32.21.. soi <br> OR <br> M2 for $\sqrt{16^{2}+22^{2}-2 \times 16 \times 22 \times \cos 115}$ <br> or M1 for $16^{2}+22^{2}-2 \times 16 \times 22 \times \cos 115$ <br> AND <br> M2 for $\frac{9 \sin 80}{\text { their }(32.21)}$ dependent on cosine rule used or M1 for $\frac{\sin A B D}{9}=\frac{\sin 80}{\text { their }(32.21)}$ |

